DESIGN TRADEOFF STUDY FOR REFLECTOR ANTENNA SYSTEMS

for the

SHUTTLE IMAGING MICROWAVE SYSTEM

Final Report 636-1

on

Contract 954026

by

R. C. HANSEN

(NASA-CR-140915) DESIGN TRADEOFF STUDY FOR N75-14940
REFLECTOR ANTENNA SYSTEMS FOR THE SHUTTLE
IMAGING MICROWAVE SYSTEM Final Report
(Hansen (R.C.), Inc., Encino, Calif.)
Unclas

Prepared for

DR. JOE WATERS

PRICES SUBJECT TO CHANGE

JET PROPULSION LABORATORY

30 August 1974

Reproduced by
NATIONAL TECHNICAL
INFORMATION SERVICE
US Department of Commerce
Springfield, VA. 22151

R. C. HANSEN, INC.

Suite 218
17100 Ventura Blvd.
Encino. Calif. 91316_x

NOTICE

THIS DOCUMENT HAS BEEN REPRODUCED FROM THE BEST COPY FURNISHED US BY THE SPONSORING AGENCY. ALTHOUGH IT IS RECOGNIZED THAT CERTAIN PORTIONS ARE ILLEGIBLE, IT IS BEING RELEASED IN THE INTEREST OF MAKING AVAILABLE AS MUCH INFORMATION AS POSSIBLE.

DESIGN TRADEOFF STUDY FOR REFLECTOR ANTENNA SYSTEMS

for the

SHUTTLE IMAGING MICROWAVE SYSTEM

Final Report 636-1

on

Contract 954026

by

R. C. HANSEN

Prepared for

DR. JOE WATERS

JET PROPULSION LABORATORY

30 August 1974

This work was performed for the Jet Propulsion Laboratory, Colifornia Institute of Technology, sponsored by the National Aeronautics and Space Administration under Contract NAS7-100.

TABLE OF CONTENTS

1.0	SUMMARY		
2.0	SYMMETRIC CASSEGRAIN ANTENNA		
	2.1	Introduction	2
	2.2	Modified J, (π u)/π u Aperture	3
	2.3	Beam Efficiency vs Taper and Blockage	6
	2.4	Reflector Back Lobes	17
	2.5	Feed Hom Pattern and Spillover Efficiency	19
	2.6	Cross Polarization Efficiency	26
	2.7	Cassegrain Design Tradeoffs	28
3.0	OFFSI	ET PARABOLOID ANTENNAS	35
	3.1	Polarization Loss	35
,	3.2	Asymmetric Amplitude Taper	36
APPEN	TOIX		39

1.0 SUMMARY

A general tradeoff is made of the symmetric Cassegrain antenna particularly with regard to the possibility of meeting a 90% beam efficiency. The factors that affect beam efficiency are aperture taper and blockage, feed cross polarization and spillover, and reflector cross polarization and backlobes. Such tradeoffs have not appeared before due to the large number of variables involved - 4 to specify a Cassegrain and several more for the feed. To allow a meaningful yet simple tradeoff, the effects of aperture taper and blockage are calculated using an adjustable sidelobe circular distribution, the Modified $J_1(x)/x$. Numerical integration is used. For the feed spillover calculation, a low sidelobe symmetric feed pattern is used with the equivalent parabola and numerical integration. Reflector cross polarization is calculated using double numerical integration. Reflector back lobes are estimated from radiation pattern envelopes of commercial common carrier dish antennas. To maintain dish and feed back radiation (90 to 180 deg.) and feed cross-pol power each below 1/2% will require careful design. The main reflector will need a heavy edge taper and may need absorber at the edge. The feed horn will also need special design treatment and may need some absorber on the horn exterior.

The curves allow a range of f/D to be determined for a specified edge taper and blockage diameter ratio. With a table of Cassegrain geometric parameters, a range of possible designs that meet the 90% beam efficiency is obtained. Use of a low magnification (M = 1.5) allows smaller feed horn diameters (typically 1.25 λ), but the feed center is close to the sub-reflector. A larger magnification (M = 3 to 5) will move the feed center back toward the main reflector apex but requires larger (typically 3.4 λ) feed diameters. In the latter case, satisfactory designs are feasible with f/D from at least .3 to .5. The actual antenna design should include GTD calculations so that the reflector and sub-reflector diffraction may be included.

Thus a symmetric Cassegrain can be designed to yield 90% beam efficiency, but the feed and reflector design and implementation must be carefully done.

2.0 SYMMETRIC CASSEGRAIN ANTENNA

2.1 Introduction

The objective of this part of the study is to determine whether a symmetrical Cassegrain antenna with appreciable blockage can provide a beam efficiency (power between main beam nulls) of 90% or more with cross polarization below -20 db. Components of energy outside the main beam are:

aperture taper and blockage (these affect sidelobes)
feed spillover including back lobes
feed cross-pol
reflector back lobes
reflector cross-pol

Specification of a Cassegrain requires 4 parameters, and typical feeds require 2 to 3 additional parameters. Thus the major task in any tradeoff is to reduce the number of variables. This is accomplished by studying the effects of aperture illumination taper and aperture blockage on an aperture distribution, where the main reflector has been simulated by the distribution. For this purpose a new, highly efficient, and low Q circular aperture distribution is used. Feed spillover and reflector cross-polarization are evaluated using the equivalent parabola, and a single parameter feed. Thus for the first time a set of general tradeoffs for beam efficiency, and as a by-product (directivity) efficiency, are obtained, giving general capabilities of the Cassegrain system.

In the next section the new distribution is discussed. Following sections cover the taper and blockage beam efficiency calculation.

2.2 Modified J₁ (γ u)/γ u Aperture

Circular aperture distributions used in texts and papers are almost always chosen because they can be readily integrated. For example, the $(1-\rho^2)^n$ on a pedestal is common. 1,2,3,4 The Gaussian is of use only for very heavily tapered apertures where the truncation is not serious, but represents a very inefficient distribution. All of these distributions suffer two major disadvantages. First, there is no simple way of choosing optimum parameters, e.g. maximum efficiency for a given sidelobe level. And second, there is no simple way of finding the parameters to yield a given sidelobe level. Both these limitations are removed in a new circular distribution, the Modified J_1 (π u)/ π u. This is related to the Modified sin π u/ π u line source developed by Taylor.

Uniform amplitude over a circular aperture gives a J_1 (π u)/ π u pattern, where $u = D \sin \theta / \lambda$. Throughout constant phase is assumed to exclude supergain. Sidelobes are - 17.6 db, and the sidelobe envelope decays as 1/u. This latter item is important as the far out sidelobes (large u) must decay as 1/u to allow a well behaved aperture distribution and low Q. Otherwise the distribution tends to have edge peaks, and the energy storage becomes large. Taylor, in developing the Modified $\sin(\pi u)/\pi$ u line source, adjusted the close in zeroes of the pattern function to reduce the corresponding sidelobes, thereby increasing the sidelobe ratio, while leaving alone the farther out zeroes which produce the 1/u envelope. A similar procedure has been followed by Hansen for the circular aperture. The pattern function

^{1.} R. C. Hansen, "Microwave Scanning Antennas," Vol. 1, Academic Press, 1964, p. 64.

A. F. Sciambi, "The Effect of the Aperture Illumination on the Circular Aperture Antenna Pattern Characteristics," report, 1964, RCA

^{3.} J. P. Grantham, "The Secondary Characteristics of the Circular Aerial for a Range of Theoretical Uniphase Aperture Distributions," TN NX-53-2, January 12, 1954, ASRE, England.

^{4.} S. Silver, "Microwave Antenna Theory and Design," McGraw-Hill, 1949.

^{5.} R. C. Hansen, op cit, Vol. 1, p. 58.

^{6.} Unpublished data.

$$E(\theta) = \frac{J_1(\pi \sqrt{u^2 - H^2})}{\pi \sqrt{u^2 - H^2}}$$

where again $u = D \sin \theta / \lambda$ and H is a constant that adjusts the sidelobe ratio. For u < H the pattern (part of the main beam) is given by

$$E(\theta) = \frac{I_1(\pi \sqrt{H^2-u^2})}{\pi \sqrt{H^2-u^2}}$$

and the sidelobe ratio is

$$5LR = 20 \log \frac{I_1(\pi H)}{\pi H} + 17.58 db$$

This Modified $J_1(\pi u)/\pi u$ distribution has the proper 1/u sidelobe envelope behavior, and because it is chosen to give the proper pattern zeroes, it 'fits the physics'. It is thus an efficient and easily used distribution. Parameters are given in the tables. The Modified $J_1(\pi u)/\pi u$ distribution itself is a monotonic function with an edge pedestal.

	71	u)/ 😙 u PARAMETER	
SLR	Н	taper efficiency	relative beamwidth
17.58 db	0	1	1
20	.4872	.980	1.0483
25	.8899	.870	1.1408
30	1.1977	.762	1.2252
35	1.4708	.668	1.3025
40	1.7254	.595	1.3741

PATTERN ZEROES	S AND PEAKS
$\gamma \sqrt{n^2 - H^2}$	type
3.8317	zero
5.1356	peak
7.0156	zero
8.4172	peak
10.1735	zero
11.6198	peak
13.3237	zero
14.7960	peak
16.4706	zero

2.3 Beam Efficiency vs Taper and Blockage

This parameter, $\ensuremath{\eta}$ beam, is defined as the fraction of radiated power that is contained in the main beam, null-to-null. To avoid a multi-dimensional tradeoff, the equivalent parabola concept is used. The figure shows the geometry. This equivalent parabola has the same diameter as the main reflector, and the same focal angle as the sub-reflector. Calculations using the equivalent parabola do not exactly match experimental results for two reasons: the sub-reflector edge diffraction is omitted; the sub-reflector may not be large in wavelengths. Thus for actual design of a Cassegrain antenna, more accurate methods are used. However, for capability tradeoffs, the equivalent parabola is adequate, and it reduces the 4 parameters to just two: D/λ and f/D. For the main reflector

$$\tan \frac{\theta_e}{2} = \frac{1}{4 + f/D}$$

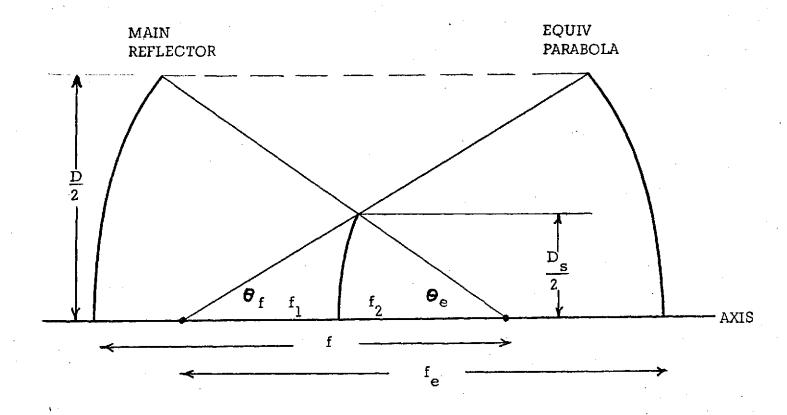
and for the equivalent parabola

$$\tan \frac{\theta_f}{2} = \frac{1}{4 \text{ fe/D}}$$

The magnification M is the ratio of focal lengths:

$$M = \frac{f_1}{f_2} = \frac{f_e}{f}$$

^{1.} P. W. Hannan, "Microwave Antennas Derived From the Cassegrain Telescope," Trans. IRE, Vol. AP-9, March 1961, pp. 140-153.



Cassegrain Reflector

After the sub-reflector diameter $\mathbf{D}_{\mathbf{S}}$ is chosen, the hyperbola focal lengths can be calculated:

$$f_1 = \frac{f_e D_S}{D} \left[1 - \frac{\tan \frac{\theta_e}{2} + \tan \frac{\theta_f}{2}}{\cot \frac{\theta_e}{2} + \cot \frac{\theta_f}{2}} \right]$$

$$f_2 = \frac{f Ds}{D} \left[| - | | \right]$$

This equivalent parabola will be used in the feed spillover calculations of a later section. For taper and blockage effects, the equivalent parabola is replaced by a circular aperture distribution, the Modified $J_1(x)/x$ of Section 2.2. Now the beam efficiency vs sidelobe ratio and the effects of blockage can be calculated using the circular aperture. The taper efficiency η_1 is

$$\eta_{t} = \frac{2E_{o}^{2}}{\frac{\pi^{2}b^{2}}{\lambda^{2}} \int_{0}^{\pi/2} E^{2} \sin \theta \, d\theta}$$

and the beam efficiency is

$$\eta_{beam} = \frac{\int_{0}^{\theta_{e}} E^{2} \sin \theta \, d\theta}{\int_{0}^{\pi h} E^{2} \sin \theta \, d\theta}$$

Circularly symmetric patterns are assumed. Blockage is usually a small part of the aperture diameter D, so the aperture distribution is nearly constant over the blockage diameter D_{b} . This diameter is that of the sub-reflector increased to include support blockage. An often used and good approximation is for uniform amplitude blockage, which gives a pattern

$$\frac{2D_{be}^{2}J_{1}(\pi u_{b})}{D^{2}\pi u_{b}}, \quad u_{b}=\frac{D_{be}}{\lambda}\sin\theta$$

This pattern is subtracted from the aperture pattern to include blockage effects.

Now the first null is shifted to a smaller value of u, called u_{o} , where u_{o} is the solution of:

$$\frac{J_1\left(\pi J u_0^2 - H^2\right)}{\pi J u_0^2 - H^2} = \frac{E_0 D_{bl}^2 J_1\left(\pi u_b\right)}{D^2 \pi u_b}$$

and the main beam peak E is given by:

$$E_o = \frac{\pm_I (\pi H)}{\pi H}$$

For low sidelobe designs, the blockage can change the null position appreciably, and thus the perturbation method first tried was discarded. In the computer code, the equation above is solved for U_o using a Wegstein root finding subroutine for each blockage and sidelobe ratio case. Null shifts will be given later.

Unfortunately, integrals of the type above can only be solved by numerical integration. And because of many sidelobes with interspersed zeroes, either a high order integration process or many points are needed. After some experimentation a Romberg 6th order integration was used, with the aperture size increased until the results converged. Library subroutines were used for Romberg and for the Bessel functions. The code is given in the Appendix.

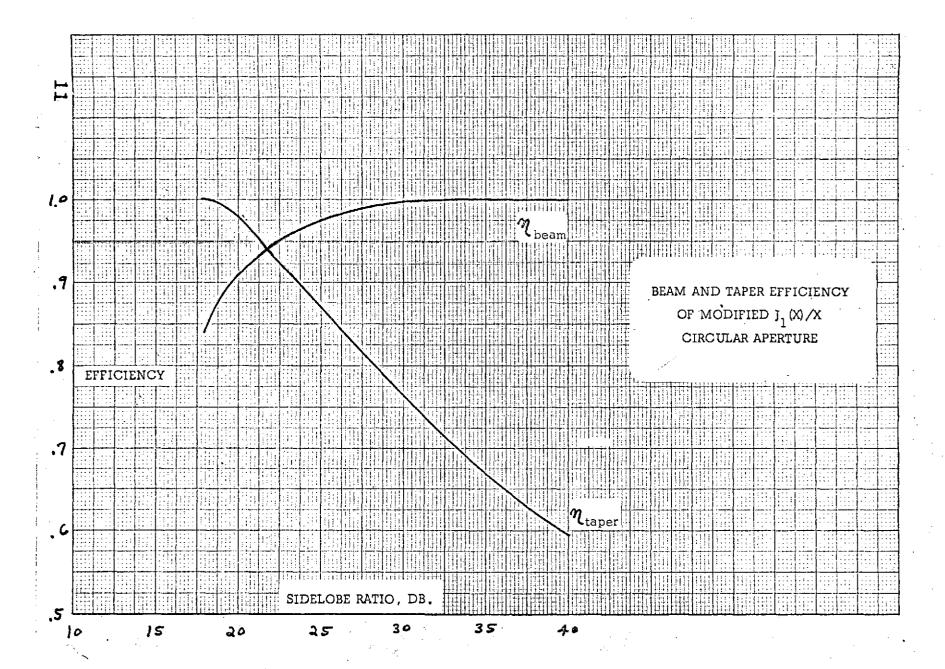
For a non-blocked aperture the beam and taper efficiencies are given in the figure vs sidelobe ratio, which is the ratio of main beam peak to first sidelobe. It can be seen that a 20 db SLR gives 91% beam efficiency and 25 db SLR gives 97% beam efficiency. With circular blocking, the beam efficiency of course drops, as shown in the second figure. Here η beam is plotted against blocking diameter/aperture diameter. These results allow the fraction of energy outside the main beam due to blockage and taper to be determined.

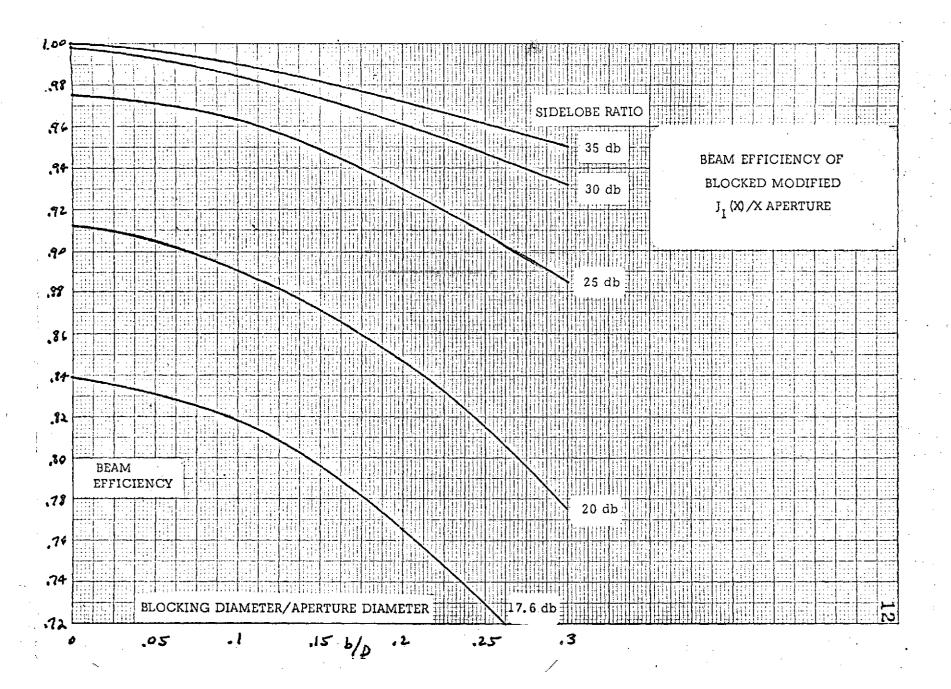
Taper efficiency, which gives directivity when multiplied by $(\pi D/\lambda)^2$, and the null shift are given in tables. Note that the blockage moves the first null closer in, and that the taper efficiency actually increases with blockage for low sidelobe levels. This is because the main beam is narrowing faster than the peak field squared is decreasing. Since the narrower main beam and higher sidelobes make the pattern more like that of a uniform aperture, it is not surprising that the η increases.

Because the Modified $J_1(x)/x$ aperture distribution is not yet available in functional form, the relation between sidelobe ratio and edge taper is obtained from another distribution, the $(1-\rho^{-2})^n$ on a pedestal. Using available raw data, the optimum n and pedestal are picked for each SLR. Results are shown in the figure. An estimate

^{*} Romberg is an adaptive trapezoidal integrator.

^{1.} A. F. Sciambi, op cit.





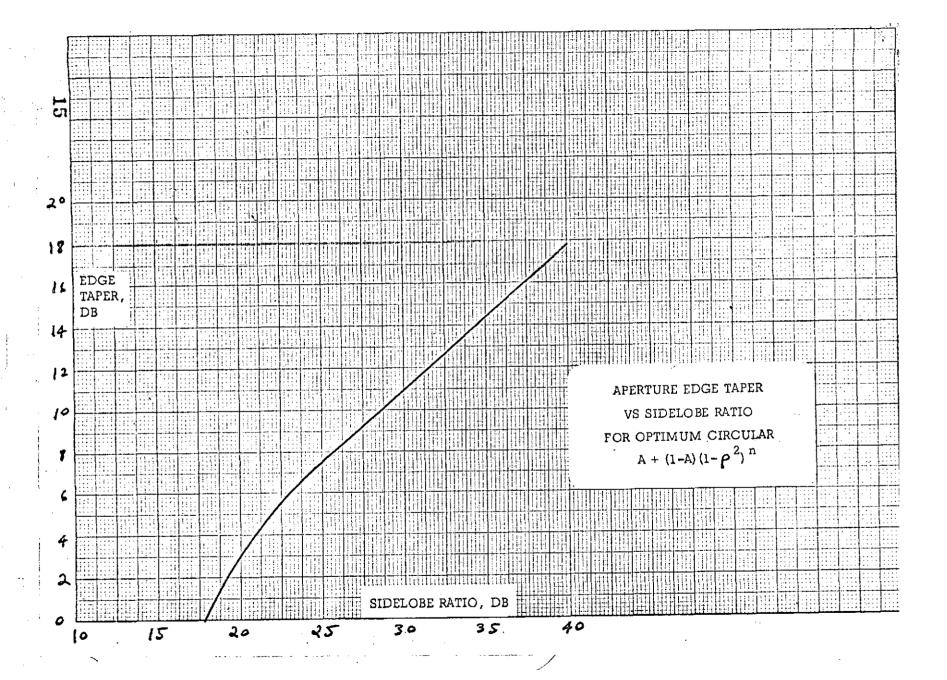
APPROXIMATE TAPER EFFICIENCY

SLR		D _s /D		
	0	.1	.2	.3
17.6	1.000	.99	.96	.91
20	.98	.97	.95	.90
25	.87	.87	.88	.89
30	.76	.76	.78	.80
35	. 67	. 67	. 69	.71

FIRST NULL REDUCTION

D be /D

SLR	.1	.2	.3
17.6	1.2%	4.4%	8.6%
20	1.6	5.6	10.9
25	2.7	9.3	17.2
30	4.7	15.1	26.8
35	7.9	24.0	41.4



of the errors can be obtained by comparing these results with the Taylor circular source l with \bar{n} equal level sidelobes.

SLR	$A + (1-A)(1-\rho^{2})^{n}$ edge taper	Taylor edge taper	
25 db	- 7.5 db	- 8.1 db	
30	-11.0	-11.5	
35	-14.4	-14.6	

The $(1-\rho^2)^n$ values are used as it is expected to be closer to the $J_1(x)/x$ values.

Now through the previous curves, giving $\eta_{\rm beam}$ vs SLR, and this curve, the $\eta_{\rm beam}$ is related to edge taper, a convenient parameter for characterizing feed patterns.

Shaping of the sub-reflector and consequent phase correction of the main reflector is sometimes used to obtain higher efficiency. 2,3 However, this is accomplished by reducing spillover and making the illumination more nearly uniform. This increases the sidelobes and correspondingly does not result in a good beam efficiency. Thus shaping is not recommended for radiometer applications.

^{1.} R. C. Rudduck, D. C. F. Wu, and R. F. Hyneman, "Directive Gain of Circular Taylor Patterns," Rad. Sci., Vol. 6, No. 12, Dec. 1971, p. 1117.

^{2.} W. F. Williams, "High Efficiency Antenna Reflector," The Microwave Journal, July 1965, pp. 79-82.

^{3.} V. Galindo, "Design of Dual-Reflector Antennas with Arbitrary Phase and Amplitude Distributions," IEEE Trans., Vol. AP-12, July 1964, pp. 403-408.

2.4 Reflector Back Lobes

Back lobes (90 to 180 deg.) of any reflector are largely controlled by the edge diffraction and by other diffracting structure such as support members. Here the edge illumination plays a key role in that a heavier taper yields lower back lobes. Typical back lobe power is obtained from radiation pattern envelopes; these are available for both conventional focus fed parabolic antennas, and those with edge 'blinders'. The latter have a much lower back lobe level. An example is taken of a 12 ft. dish at 11.2 ghz, with efficiency of 52%. The measured gain of 49.8 db (D/ λ = 136.6) gives a total integral of E² of:

$$\int_{0}^{\pi} E^{2} \sin \theta \, d\theta = 2.09 \times 10^{5}$$

Since the RPE consists of straight lines, an approximate integration from 90 to 180 deg. is easy. For the conventional and edge treated dishes the results are:

DISH	RPE no.		power in back lobes
ordinary	3111	$.38 \times 10^{-5}$	18%
edge shield	3177	1.02×10^{-7}	.5%

Although these are not Cassegrain, the results are expected to be the same. See RPE's in Appendix. Thus the conclusions are that a heavy edge taper, or an edge shield, is necessary to reduce back lobe power below 1%. Of course when the antenna is pointed away, at most only part of the back lobes see the hot earth so this mitigates the back

Andrew Corp. radiation pattern envelopes (RPE).

lobe problem. For the actual antenna design, a GTD * calculation of back lobe energy should be made.

^{*} Geometric Theory of Diffraction.

2.5 Feed Horn Pattern and Spillover Efficiency

The ideal feed horn should have a circularly symmetric pattern to give equal ${\bf E}$ and ${\bf H}$ plane patterns and should have a parameter controlling beamwidth. A representative pattern ${\bf I}$ is

$$E_f = (1 + \cos \theta) \frac{J_1(x)}{x}$$
, $x = \frac{\pi D_f}{\lambda} \sin \theta$

where the feed diameter $D_{\mathbf{f}}$ controls the beamwidth. The (1 + cos $\boldsymbol{\theta}$)/2 factor is the reflector path loss function; 2 J_1 (x)/x is unity at x = 0. This feed pattern will be used to calculate feed spillover and cross-pol losses. A convenient way of characterising the feed is by edge taper. Values of D_f and $\boldsymbol{\theta}_f$ giving specific values of edge taper are obtained using a root finder to determine x (in the equation above) for a given $\boldsymbol{\theta}_f$ and E_f ; see appendix. The table gives D_f/λ_f for $\boldsymbol{\theta}_f = 20$ (5) 90 and for $E_f = -10$ (2) -18 db, which covers the practical range of edge tapers. Using this feed pattern to determine spillover efficiency (and cross-pol efficiency) vs edge taper (relatable to sidelobe ratio) and reflector angle $\boldsymbol{\theta}_f$ again requires numerical integration:

$$\eta_{spill} = \frac{\int_{0}^{\theta_{f}} E^{2} \sin \theta \, d\theta}{\int_{0}^{\pi/2} E^{2} \sin \theta \, d\theta}$$

^{1.} A. W. Rudge and M. Shirazi, "Investigation of Reflector-Antenna Radiation," Final Report on Contract No. SC/11/73/HQ, Univ. of Birmingham, June 1974.

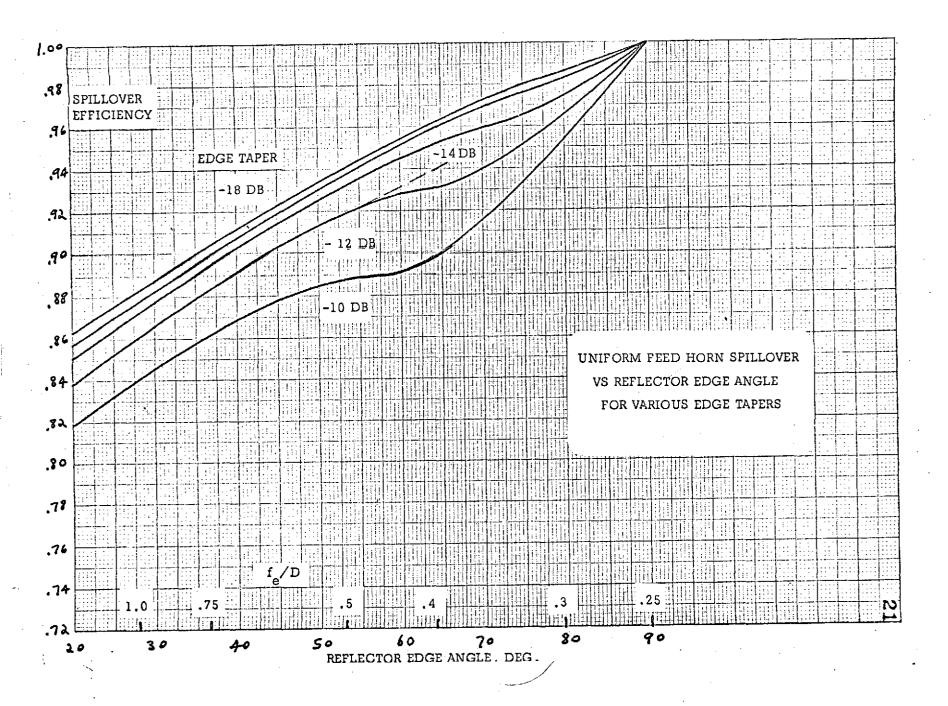
Feed energy past 90 deg. will be estimated separately, as the external structure strongly affects this part of the feed pattern. Now the results will contain oscillations; for a fixed dish edge angle $\boldsymbol{\theta}_f$ as D_f changes the number and fraction of feed pattern sidelobes included changes, giving a fine structure which tends to obscure the results. Since feed sidelobe structures are highly variable, the effects of these particular ones can be eliminated by using the integrated sidelobe envelope.

The sidelobes cannot be integrated, even without the sin $\Theta \& \Theta$ which makes the result dependent upon D. However, the power of a single sidelobe can be approximated by an envelope, provided sin $\Theta \simeq$ constant. The single sidelobe power is approximated by the envelope power:

$$\int_{X_1}^{X_2} \left(\frac{2 \mathcal{J}_1(x)}{x} \right)^2 d\mu = \mathcal{L} \int_{X_1}^{X_2} \frac{8 \mathcal{L}_1}{\pi x^3}$$

Numerical (Romberg) integration is used to determine the value of the constant \angle . From the table it appears that \angle \longrightarrow .5, and it is suspected that use of the asymptotic form of the Bessel function in the integral above (without $\sin \theta$) can be directly integrated to give \angle = .5. Now that \angle is known, the envelope as a function of θ , together with $\sin \theta$, can be numerically integrated. This somewhat devious process allows more rapid numerical integration, and more important, will remove oscillations from the spillover data.

Using the feed horn pattern just described and the envelope thereof, the spillover is calculated at increments in reflector edge angle of 5% with the appropriate feed diameters used for each angle to give the edge taper values of -12 (to) -18 db. Romberg integration is again used to calculate the total energy and the energy impinging upon the reflector. The latter integration is divided into two parts where the feed pattern weighted sidelobe envelope meets the main beam. In the figure is shown the spillover efficiency vs reflector edge angle for the five different edge taper cases. The change



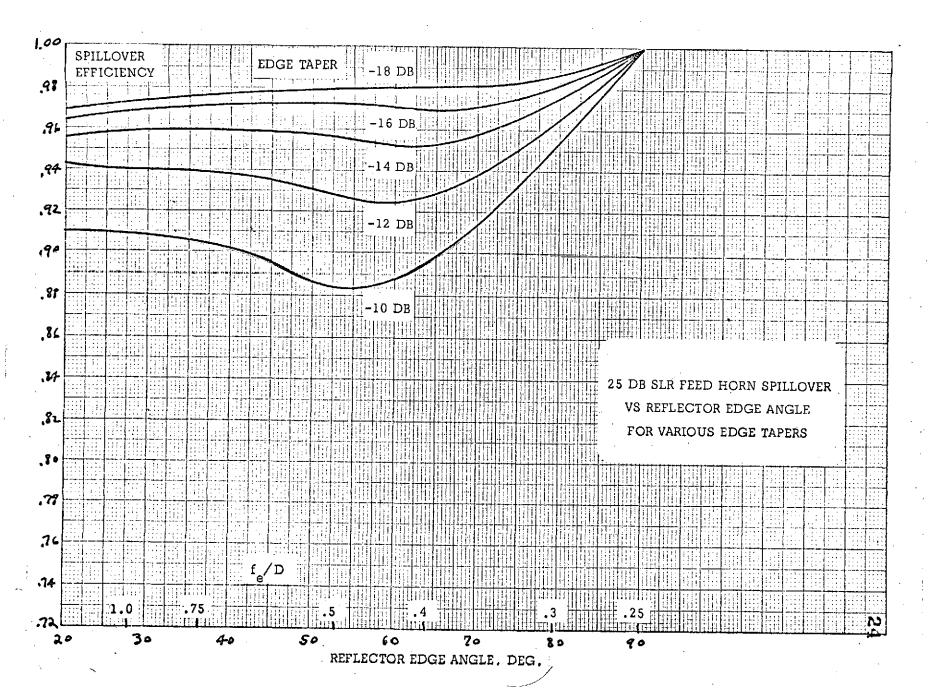
ENVELOPE COEFFICIENT

n	< <	error
1	.48256	3.4 %
2	.49263	1.4
3	.49599	.74
4	.49749	.44
5	.49828	.28
6	.49875	.19
10	.49950	.04

in shape of the curves occurs when the feed pattern main beam to weighted envelope transition occurs at the edge of the dish. This occurs for u = .968; see code in Appendix. It should be recalled that actual feed patterns with discrete sidelobes will produce curves containing considerable fine structure. However, these envelope curves are more useful for design tradeoffs.

In a subsequent section, it appears that the achievement of 90% efficiency is limited by the feed spillover. Thus a feed with low sidelobes must be used. An approximate calculation of the performance of a typical feed of this type is obtained by using the $J_1(x)/x$ distribution for the feed horn. Here the constant H is chosen for 25 db feed SLR and for each reflector edge angle the feed diameter is chosen to provide the specified reflector edge taper as before. The new feed pattern envelope has a different intersection with the main beam, which is also recalculated. The only approximation occurs wherein the constant alfa which relates the power in a sidelobe to the integral of the envelope power is taken from the uniform feed case. For large feed horns, this represents a small error and in any case gives a rapid and useful answer. Again the spillover integrals are calculated with the new feed pattern and envelope and the results are shown in the figure. Since the sidelobe envelope now contributes a small amount of power, one might expect the spillover efficiency to be somewhat constant until the reflector edge angle is sufficiently large that the only remaining sidelobe starts disappearing. This is in fact the case for edge tapers of 15 db or more. However, for smaller edge tapers, the main beam power changes with reflector angle also, because of the square root argument that now appears in the $J_1(x)/x$. Thus the important conclusion that for this type of low sidelobe feed, and probably for all conventional low sidelobe feeds, edge tapers in the 15 db or more range are indicated. So called 'high efficiency' feeds, where a large feed aperture with many modes is used to provide nearly uniform reflector illumination with very low feed sidelobes, are not of interest here, as their beam efficiency is close to that of a uniformly illuminated aperture, i.e. 84% or worse, depending upon blockage.

The calculations for beam efficiency and spillover have included the feed pattern out to 90 deg. This is because the back lobes of a feed are not only dependent



upon the specific feed but also upon the physical structure including supports and all material in the vicinity of the feed. Thus calculation of feed back lobe is both difficult and somewhat irrelevant until a final feed and reflector geometry, including all supports, cables, dielectric members, etc., are fixed. A satisfactory procedure is to estimate the percentage of power in the back lobes of a reasonable feed. Using multimode or corrugated horn feeds, the back lobe energy can be expected to be of the order of .5%. However, dipole array feeds typically will have much higher back lobe energy due to diffraction around the ground plane edges. Feed cross polarized energy must be considered, of course, but has not been calculated here, as it is completely dependent upon the particular type of feed.

2.6 Cross Polarization Efficiency

The definition used here for cross polarization power is that using spherical coordinates. ¹ The integral is ²

$$\eta_{\chi} = \frac{\left| \int_{0}^{\pi/2} \int_{0}^{\theta_{f}} E(\theta) \frac{\cos \theta \sin^{2} \theta + \omega z^{2} \theta}{\sqrt{1 - \sin^{2} \theta \sin^{2} \theta}} + \tan \frac{\theta}{a} d\theta d\theta \right|^{2}}{\left| \frac{\pi}{a} \int_{0}^{\theta_{f}} E(\theta) + \tan \frac{\theta}{a} d\theta \right|^{2}}$$

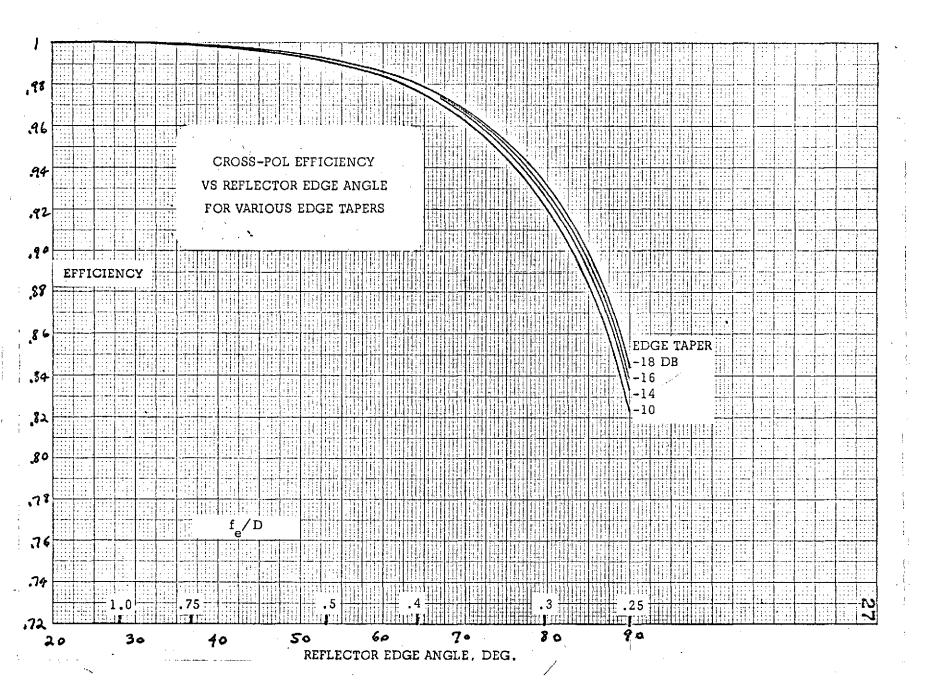
Here the same feed pattern used for spillover calculations is used. Since reflector cross polarization is zero in the principal planes, the double integration is required; and this is performed with a double Simpson. The co-pol power is obtained with a Romberg integration. Since only the main beam of the feed pattern illuminates the reflector, the question of feed pattern sidelobe vs envelope is not germane. The appendix shows the computer code used for this calculation. The set of equivalent feed diameters and reflector edge angles corresponding to edge tapers of -10, -12, -14, -16, and -18 db were inserted into the program. The Figure shows the cross polarization efficiency as a function of feed edge angle for these several edge tapers. It is interesting to note that for an equivalent parabola f_e/D of .5, the loss is about 1%; whereas for $f_e/D = .35$, the loss is about 4%. These results compare favorably with those calculated for a variety of feed patterns by Rudge. 3,4,5

^{1.} A. C. Ludwig, "The Definition of Cross Polarization," Trans. IEEE, Vol. AP-21, January 1973, pp. 116-119.

^{2.} R. E. Collin and F. J. Zucker, "Antenna Theory, Part II," McGraw-Hill, 1969, Chap. 17.

^{3.} A. W. Rudge and M. Shirazi, "Investigation of Reflector-Antenna Radiation," Interim Report on Contract No. SC/11/73/HQ, Univ. of Birmingham, October 1973.

^{4.} A. W. Rudge and M. Shirazi, "Investigation of Reflector-Antenna Radiation," Final Report on Contract No. SC/11/73/HQ, Univ. of Birmingham, June 1974.



2.7 Cassegrain Design Tradeoffs

Due to the multidimensionality of the design problem, it is not feasible to have a single tradeoff expression or curve. Rather a beam efficiency budget is constructed from the several components and the parameters are varied until the beam efficiency reaches (or does not reach) a satisfactory level. Note that there is no mention of optimizing beam efficiency. It is probably more effective from a systems standpoint to maximize a combination of gain and inverse beamwidth while maintaining a satisfactory beam efficiency.

The major constituents to beam efficiency as previously discussed are:

aperture taper blockage feed spillover polarization loss

To start, a combined reflector back lobe power, feed back lobe power, and cross polarization power of 1% is assumed. Meeting this stringent requirement involves either a low edge taper or edge treatment for both the reflector and the horn and careful attention to polarization purity in the horn. A cut and try process using the curves previously presented is now performed for several edge tapers and for several blockage diameter ratios. The results are quite pessimistic and show that there is a very narrow range of edge angles that gives an overall 90% beam efficiency. For example, the following table shows taper, spillover, and cross-pol values for a blockage ratio of .1 for the three tapers shown.

Blockage I	Diameter	Ratio =	.1
------------	----------	---------	----

edge taper	taper efficiency	spillover efficiency	cross-pol efficiency	edge angle
-16 db	.993	.920	.996	46 deg
-14	.989	.925	.995	50
-12	.988	.930	990	59

With a blockage ratio of .15, a solution is just possible for a -16 db, 50 deg. edge and for a -14 db, 56 deg. edge. For a blockage ratio of .2, the -16 db, 54 deg. edge is just possible. Since none of the calculations herein have included reflector and sub-reflector edge diffraction, there does not seem to be a feasible Cassegrain solution using the uniform feed model.

As mentioned before, the low sidelobe feed considerably improves the situation. Because of the considerably better spillover efficiencies, a range of angles is now feasible. In each case, the design is possible down to the lowest edge angle calculated, 20 deg. The maximum edge angle is shown in the following table. Because of this latitude, an intermediate value can be chosen to allow for the unincluded diffraction effects. Also the heavier edge tapers will give less power in the back lobes. The correspondingly large feeds, however, may interfere with each other since feeds are needed for several frequencies, and in all cases the feed should not be bigger than the equal blockage feed size.

Maximum Edge Angle

	E DIOOR	age Diamoter i	
Edge Taper	1	.15	.2
-16 db	77 deg.	76	73
-14	72	66	61
-12	53	46	~ 30

Blockage Diameter Ratio

Thus for modest blockage (.1) or less, there is a range of edge angles of from 20 deg. (or even less) to about 60 deg., with edge taper in the -14 to -16 range. To allow the smallest diameter feed, the -14 db number is chosen here.

Next the Cassegrain parameters are examined to see if a practical design will fit the restrictions. The feed diameter (including all feeds) should be no larger than the 'minimum blockage' criterion l wherein the feed blockage equals the sub-reflector blockage. Calling the feed diameter $\mathbf{D}_{\mathbf{f}}$, the minimum blockage value is

$$\frac{Df}{Ds} = \frac{(f_1 + f_2)/f}{\frac{1}{2} + \frac{1}{2} \sqrt{1 - p_s^2/f^2}} \simeq \frac{f_1 + f_2}{f}$$

The frequencies of primary concern are:

channel 5	freq. =	20.5 ghz	D/X	-=	273
6		22.2			296
7		31.4			419
8	-	52.9			705
9		94			1253
10		116			1547

Typically channels 5 and 6 will have a single horn, with the channels 7 and 8 horns adjacent. The last two will be either coaxial with a lower frequency horn or located among the others. So the net feed diameter will be roughly 1.5 times that of channel 1. Taking the -14 db edge taper, and edge angles of 20 and 60 deg. as design extremes gives:

6 f	${}^{\mathrm{D}}\mathrm{_{f}}/\lambda$	D _f /D	D _f /D	f _e /D
	ch. 5	ch. 5	total	
20	3.35	.01226	.0184	1.418
60	1.24	.00454	.00681	.433

^{1.} P. W. Hannan, op cit

^{*} This would minimize the offset (in wavelengths) for any one feed.

To assist in determining the blockage diameter ratio and $(f_1 + f_2)/f$, a table of parameters is given in the Appendix. The parameter $(f_1 + f_2)/f$ is important as it determines where the feed phase center is located between the main reflector vertex and the subreflector. If $(f_1 + f_2)/f = 1$, the feed center is at the main reflector vertex. The feed diameter is readily obtained by multiplying together the first and last columns:

$$\frac{D_f}{D} = \frac{D_s}{D} \cdot \frac{f_1 + f_2}{f}$$

Several examples will illustrate the possible sets of parameters:

Case 1

Take the largest edge angle, $\theta_{\rm f} \simeq 60$ deg. or $\frac{f_{\rm e}}{D} = .45$.

For this case, small magnification is needed, say M=1.5. Then f/D=.3

$$\frac{D_f}{D} \simeq .007$$

Values that provide feed blockage ≤ sub-reflector blockage are:

$\frac{D_s}{D}$	$\frac{f_1 + f_2}{f}$	minimum blockage D _f /D	
.075	.100	.007	
.1	.134	.0134	
.15	.201	.0302	

In this case, the main reflector f/D=.3 but the feed point is located close to the sub-reflector.

Case 2

Take the smallest edge angle, $\theta_{\rm f} \simeq 20$ deg., $\frac{{\rm f}_{\rm e}}{{\rm D}} = 1.5$.

Actually smaller angles can be used but require even larger feed diameters. Take M=5, so f/D=.3.

$$\frac{D_f}{D} \simeq .02$$

Acceptable values are:

$\frac{D_s}{D}$	$\frac{f_1 + f_2}{f}$	minimum blockage $\mathrm{D_{f}^{/D}}$
.065	.335	.02
.1	.517	.05
.15	.775	.12
.2	1.033	.21

A blockage of .1 and feed point .517f is a reasonable design.

Case 3

Again the small edge angle,
$$f_e/D = 1.5$$
 but $M = 3$. $f/D = .5$. $\frac{D_f}{D} \approx .02$

Acceptable values are:

$\frac{D_s}{D}$	$\frac{f_1 + f_2}{f}$	minimum blockage $\mathrm{D_{f}^{/D}}$
.075	.275	.02
.1	.367	.014
.15	.550	.08
.2	,733	.15

Here are also reasonable designs, with the main reflector f/D larger than Case 2 but with a feed center closer to the sub-reflector for a given blockage ratio. For example, a blockage of .15 and feed point .550 f is practical.

These three cases are now compared in terms of beam efficiency, using in each case the sub-reflector diameter representing minimum blockage even though the feed distance is small. The following table gives the pertinent parameters.

	Case 1	Case 2	Case 3
f /D	.45	1.5	1.5
f _e /D M	1.5	5	3
f/D	.3	.3	.5
D _s /D	.075	.065	.075
$(f_1 + f_2)/f$.100	.335	.275
6 e	58 deg.	19 deg.	19 deg.
↑ taper	.993	.994	.993
η spill	.953	.955	.955
n spili n xp	987	1.000	1.000
n Ay N beam	.925	.940	.939

edge taper = - 14 db dish and feed back lobes and feed cross-pol = 1%

It can be seen that the performance with large feed (f_e/D large) is somewhat better, and the feed distance is also more manageable. The tradeoff between main reflector f/D appears to be more nearly that of space and construction.

If the band 5-6, band 7 and band 8 feeds are clustered in a triangular configuration, with the focus of the reflector located just outside each feed horn edge (between the 3 horsn), the offset of each beam varies depending on the f/D, $D_{\rm S}/D$,

etc. In all three cases, the offset is 4 beamwidths or less, and this allows good sidelobe control. The Case 3 with f/D = .5 is better, and Case 1 with low magnification is better yet. However, all are acceptable.

3.0 OFFSET PARABOLOID ANTENNAS

3.1 Polarization Loss

The offset reflector can have negligible polarization loss if the feed axis is maintained parallel to the paraboloid axis. But of course the feed must be tipped, with the feed angle approximately half the edge angle, to reduce spillover and to provide the proper aperture taper. Polarization loss has been calculated for offset reflectors by Dijk et al. 1 For an edge angle of 60 deg. (f/D = .433), the cross-pol efficiency is .98 for polarization parallel to the offset direction and .97 for polarization perpendicular. These numbers compare with a cross-pol efficiency of 1.00 for the symmetric Cassegrain cases. Thus for the offset reflector to be a candidate, the spillover and taper efficiencies together must be higher than for the Cassegrain.

^{1.} J. Dijk, et al, "The Polarization Losses of Offset Paraboloid Antennas," IEEE Trans., Vol. AP-22, July 1974.

3.2 Asymmetric Amplitude Taper

The offset reflector, of course, has no blockage; for the Cassegrain cases considered, the blockage accounts for less than 1% degradation of beam efficiency. On the other hand, the offset reflector has a serious difficulty, the asymmetric amplitude distribution produced by the geometry. The limited scope of this investigation did not permit the extensive two-dimensional numerical integration analysis necessary to quantify this tradeoff, so a simple calculation is made to indicate the magnitude of the problem. A plane through the reflector and feed center in the offset direction is taken as a one-dimensional aperture. Over this aperture should be heavy edge taper (at least 14 db) to reduce edge diffraction, sidelobes, etc., and a cosine function is used to simulate this. However, in addition there is the asymmetric geometry taper which has maximum amplitude at the edge of the reflector closest to the reflector axis and minimum amplitude at the top edge. For example, with f/D = .25, the amplitude ratio is 2:1. Larger f/D's give a ratio closer to 1. The worst case is taken, f/D = .25. The basic integral is

$$F(u) = \frac{3}{5} \int \cos \frac{\pi - 2p}{8} \cos p e dp$$

where $u=(D/\lambda)$ sin θ , and β is the aperture variable. The symmetric taper is given by $\cos\beta$ and the path length asymmetric taper by $\cos^2(\pi-2\beta)/8$. The result is

$$F(u) = \frac{.6 \cos \pi u}{1 - 4 u^2} + \frac{1.2 (\sin \pi u + \cos \pi u)}{3 + 8u - 16 u^2}$$

The normal cosine taper pattern is

Calculation of the two patterns shows that the asymmetric path loss leaves the sidelobe peaks essentially unchanged, broadens the null-to-null beamwidth by about 8%, and fills in all nulls to roughly 10 to 20 db below the sidelobe peaks. None of these effects are serious, and for larger f/D will be even less. 1

With the higher polarization loss, the offset reflector appears to offer lower beam efficiency than the symmetric Cassegrain; but the 90% figure for the offset reflector seems possible.

^{1.} L. S. Wagner and K. W. Morin, "Performance of a Parabolic Antenna with an Offset Feed," memo report 2375, Dec. 1971, NRL.

APPENDIX

		page
/J1BEAM/	aperture beam efficiency	40
Radiation P	attern Envelopes	42
/BES/	sidelobe integration	44
/EDGE/	edge taper vs feed diameter	46
/SPILL/	feed spillover efficiency	48
/INTER/	envelope-main lobe intersection	49
/POL/	polarization loss	50
/CASS/	Cassegrain geometric parameters	51

Preceding page blank

/J1BEAM/

```
C
      MODIFIED J1(X)/X BEAM EFFICIENCY & GAIN
C
      WITH SYMMETRIC CIRCULAR HOLE BLOCKAGE
C
      H IS MOD J1 PARAMETER. UØ IS FIRST NULL
      COMMON H2,P,D,DBL,E
      COMMON /W/ PI.HH.EB.B
      P=PI=3.1415926536
      ZN=3.83171
      DISPLAY /
      ACCEPT "M.H.XS
                        "_M_H_XS
      H2=HH=H*H
      CALC BEAM PEAK
C
      CALL BESSEL (P*H, 1, BFIØ, IF, 3)
      E=2*BFIØ/(P*H)
      IF (P*H.LT..001) E=1
      E2=E*E
      ACCEPT "D/WV.BLOCK DIA/D
100
                                   ".D.B
C
      CALC BLOCKED NULL POSIION
      EB=E*B*B
      CALL ROOTW(U08.F0.XS.1.E-5.50,IFL)
      X\emptyset = P * SQRT (UØB * UØB - H2)
      DISPLAY XØ,FØ,IFL
      THØB=ARCSIN(UØB/O)
      DISPLAY "% NULL SHIFT
      WRITE (1.110) 100*ABS(X0-ZN)/ZN
 1Ø
      FORMAT(F8.2)
      DBL=D*B
С
      CALC WITH BLOCKED FEED
      CALL ROMBER (0. THØB .M . Y1)
      CALL ROMBER (THUB., 5*P.M.Y2)
      W=2*E2/(P*D)**2
      ETAT=W*(1-B*B)**2/(Y1+Y2)
      ETAB=Y1/(Y1+Y2)
      WRITE (1.200) ETAT, ETAB,/
      FORMAT (2F8.3)
200
      GO TO 100
      END
      FUNCTION FCT(X)
      COMMON HF.PI.DF.8F.E
      S=SIN(X)
      U2=(DF*S)**2
      IF (U2.LT.HF) GO TO 40
      ARG=PI*SQRT(U2-HF)
      IF (ARG.LT..ØØ1) GO TO 3Ø
      CALL BESSEL (ARG. 1. BFJ. IF. 1)
      FCT=2*BFJ/ARG
      GO TO 50
      FCT=1
      GO TO 50
      ARG=PI*SORT(HF-U2)
40
```

/J18EAM/

```
IF (ARG.LT..001) GO TO 70
      CALL BESSEL (ARG, 1, BFI, IF, 3)
      FCT=2*BFI/ARG
      GO TO 50
70
      FCT=E
5Ø
      AR=PI*S*BF
      IF (AR.LT..001) GO TO 10
      CALL BESSEL (AR. 1.8FJØ. IF. 1)
      FCT0=2*BFJ0/AR
      GO TO 2Ø
10
      FCT\emptyset = 1
20
      FCT0=FCT0*E*(BF/DF)**2
      FCT=S*(FCT-FCT0)**2
      RETURN
      END
      FUNCTION WFUN(X)
      COMMON /W/ PI,HH,A,B
      ARG=PI*SQRT(X*X-HH)
      CALL BESSEL (ARG. 1, BFJM, K. 1)
      AR=PI*8*X
      CALL BESSEL (AR. 1. BFJB.L. 1)
      WFUN=BFJM/ARG-A*BFJB/AR+X
      RETURN
      END
```

42

RADIATION PATTERN ENVELOPE

ANTENNA TYPE NUMBER P12-107C, P12-107D PL12-107C, PL12-107D

ANDREW

RPE 3111

S. A. Walken

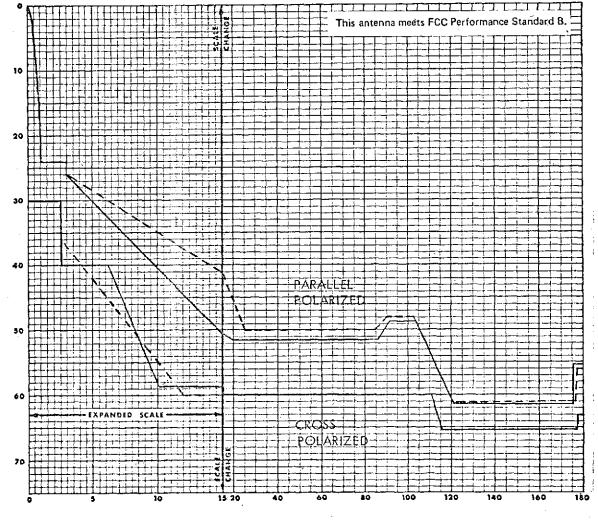
August 4, 1971

12 FOOT ANTENNA 10.7 - 11.7 GHz PLANE POLARIZED

Gain: 49.8 + 0.2 dBi at 11.2 GHz

For reference to a half wave dipole subtract 2.15 dB.

See Andrew Bulletin 1032, "Radiation Pattern Envelopes," for further information.



AZIMUTH # DEGREES FROM MAIN LOBE

Andrew Corporation 10500 W. 153rd Street Orland Park, III., U.S.A. 60462

ANTENNA DIRECTIVITY-- BOWN FROM MAIN LOBE

Andrew Antenna Company-Ltd. 606 Beech Street Whitby, Ontario, Canada Andrew Antenna Systems Lochgelly, File Great Britain Andrew Antennas 171 Henty Street Reservoir, Victoria, Australia 3073

3:0

RADIATION PATTERN ENVELOPE

ANTENNA TYPE NUMBER

HP12-1070

ANDREW

November 17, 1971

12 FOOT ANTENNA

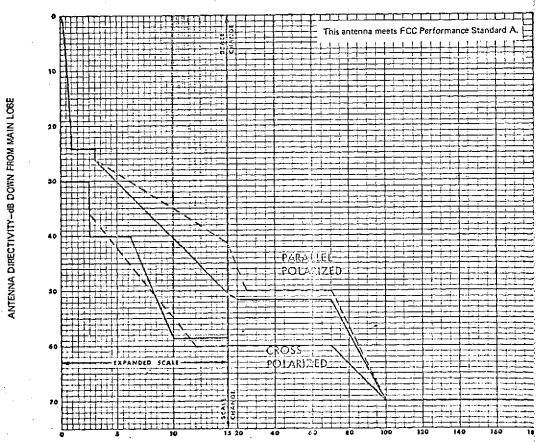
10.7 - 11.7 GHz

PLANE POLARIZED

Gain: 49.8 ± 0.2 dBi at 11.2 GHz

For reference to a half wave dipole subtract 2.15 d9.

See Andrew Bulletin 1032, "Rediction Pattern Envelopes," for further information.



AZIMUTH # DEGREES FROM MAIN LOBE

Andrew Corporation 10500 W, 153rd Street Orland Park, III., U.S.A. 60462

Andrew Anrenna Company Ltd. 606 Beach Street Whilby, Ontario, Canada Andrew Anténna Systems Lochquilly, File Great Britain Andrew Antennus 171 Henty Street Readryoir, Victoria , Australia 3973

```
OLD FILE?
12 LINES
*XTRAN
+COM
OUTPUT:
OPTIONS: PRO
+B
OPTIONS:
SPROG:
XLIBE JAN 25
X1,X2
        19.61586.22.76008
    4.23Ø522494E-Ø4
X1,X2 22.76008,25.90367
    2.789364966E-04
X1.X2 25.90367.29.04683
    1.935447211E-04
X1,X2
        29.04683,32.18968
    1.397537889E-Ø4
X1, X2 32, 18968, 35, 33231
    1.041928841E-04
X1, X2
ESC:
      ($MAIN$)Ø
+0
₩P
      BESSEL J1(X)/X SIDELOBE INTEGRATION
C
      DISPLAY
      ACCEPT "X1.X2
                      ".X1.X2
100
      CALL HOMBER(X1, X2,6,R)
      DISPLAY /.R./
      GO TO 100
      END
      FUNCTION FCT(X)
      CALL BESSEL(X,1,BF,I,1)
      FCT = (2*BF/X)**2
      RETURN
      END
```

44

-COP /BES/ TO TEL

```
BESSEL J1(X)/X SIDELOBE INTEGRATION
C
C
      ENVELOPE
      COMMON P
      DISPLAY
      P=3.1415826536
ACCEPT "N ",N
100
      CALL ROMBER((N+.25)*P.(N+1.25)*P.5.A)
      DISPLAY /,R./
      GO TO 100
      END
      FUNCTION FCT(X)
      COMMON P
      FCT=8/(P*X**3)
      RETURN
      END
```

```
EDGE TAPER VS DIAM OF J1(X)/X FEED
C
                                                       25 M 56R
C
      USES WEGSTEIN ROOT FINDER
      DIMENSION D(5)
      COMMON C.E.H.P
      DISPLAY /
      P=3.1415926536
      H=.8899
      XS=1
      DO 100 TH=20.90.5
      THR=TH*P/180
      S=SIN(THR)
      C=COS(THR)
       J = \emptyset
      DO 200 EDB=2.58,10.58.2
      1+1=5
      E = 10 ** (-.05 *EDB)
      CALL BOOTW (XW.FW.XS.1E-6.50.IFL)
      IF (IFL.EQ.Ø.AND.FØ.LT.1E-Ø5) GO TO 200
      DISPLAY "ERROR FLAG & RESIDUE
                                           '.IFL,FØ
200
      D(J) = X\emptyset/S
100
      WRITE (1,110) TH, (D(I),I=1,5)
      FORMAT (F6.0,5F8.3)
110
      DISPLAY /
      END
      FUNCTION WFUN(X)
      COMMON C.E.H.P
       AR=P*SQRT(ABS(X*X-H*H))
       IF (X.LT.H) GO TO 10
      CALL BESSEL (AR, 1, BF, I, 1)
       WF = (1+C)*BF/AR
       GO TO 20
       CALL BESSEL (AR, 1, BF, I, 3)
10
       WF=(1+C)*8F/AA
20
       WFUN=WF-E+X
       RETURN
       END
```

```
*WRI /EDGE/
OLD FILE?
36 LINES
*XTRAN
+COM
OUTPUT:
PTIONS: PRO
```

apertur diameters 25 db SLR

+R OPTIONS: SPROG:

XLIBE JAN 25

of .	-(0	-12	-14	-16	-18 der elge
20.	2.921	3.151	3.346	3.514	3.659
25.	2.349	2.537	2.697	2.835	2.953
3Ø.	1.969	2.131	2,268	2.386	2.487
35.	1.700	1.843	1.965	2.069	2.159
40.	1.499	1.629	1.740	1.835	1.917
45.	1.343	1.465	1.568	1.656	1.732
5Ø.	1.219	1.335	1,432	1.516	1.588
55.	1.117	1.229	1.324	1.404	1.473
60.	1.032	1.142	1.235	1.313	1.381
65.	0,960	1.069	1.161	1.239	1.305
70.	0.895	1.006	1.098	1.177	1.244
75.	Ø.837	0.951	1.045	1,125	1.193
80.	Ø.782	0.901	Ø.999	1.081	1.151
85.	Ø.728	0.854	Ø.957	1.043	1.116
90.	Ø.671	0.809	Ø.918	1.009	1.086

STOP* (\$MAIN\$)Ø

COP /SPILL/ TO TPT

```
REFLECTOR SPILLOVER USING A SYMMETRIC J1(PU)/PU FEED
C
C
      FEED PATTERN PAST 90 DEG NOT INCLUDED
С
      FEED SIDELOBE ENVELOPE = MAIN LOBE AT Z
C
      INSERT D(IAMETER) VECTOR FOR DESIRED EDGE TAPER
      DIMENSION D(15)
      COMMON P.DF.Z
      P=3.1415926536
      Z=3.04126
      TS=20
      TD = 5
      I = \emptyset
      M=4
      DISPLAY /
      DATA D/2.516.2.024.1.697.1.466.1.293.1.160.1.054.
200
         .967..894..832..777..728..681..634..586/
      DO 100 TH=TS.90.TD
      I=I+1
      DF=D(I)
      THR= TH*P / 180
      ARG=P*DF*SIN(THR)
      CALL BESSEL (ARG. 1.BFJ. IF. 1)
      CALL ROMBER (0. THR.M.R1)
      CALL ROMBER (THR..5*P.M.R2)
      ETA5=R1/(R1+R2)
      FOD=.25*COS(.5*THR)/SIN(.5*THR)
      WRITE (1.300) TH.FOD.ETAS
100
      CONTINUE
300
      FORMAT (F7.1,2F8.3)
      SUBROUTINE FCT(X)
      COMMON P.F.Z
      S=SIN(X)
      AR=P*F*S
      IF (AR.GT.Z) GO TO 30
      IF (AR.LT..001) GO TO 10
      CALL BESSEL (AR. 1.BF. I. 1)
      FCTØ=(1+COS(X))*BF/AR
      GO TO 4Ø
10
      FCTØ=1
      GO TO 40
      FCTØ=(1+COS(X))/(AR*SQRT(P*AR))
30
 Ø
      FCT=S*FCTØ*FCTØ
      RETURN
      END
```

*WRI /INTEH/ NEW FILE? 16 LINES *XTRAN +TEST START VAL 3 -1.018634066E-10 3.041263871 d= 1 (power) START VAL 2.5 -5.966285244E-10 3.041263869 for $\frac{2J_1(x)}{x} = \frac{2}{x\sqrt{\pi}x}$ this is START VAL 3.041263871 -13.44 dr pt. START VAL ESC: (\$MAIN\$)200+1 +COM OUTPUT: OPTIONS: SYM CORRECTED SYMBOLIC:/INTER/ OLD FILE? -COP /INTER/ TO TEL INTERSECTION OF J1(X)/X & WEIGHTED ENVELOPE C USES WEGSTEIN ROOT FINDER С 200 DISPLAY / ACCEPT "START VAL "XS CALL ROOTW(XØ,FØ,XS,1.E-5.5Ø,IFL) IF (IFL.EQ.Ø) GO TO 100 DISPLAY "ERROR FLAG ", IFL DISPLAY XØ.FØ./ 100 GO TO 200

END

RETURN END

FUNCTION WFUN(X) P=3.1415926536

CALL BESSEL(X,1,8FJ,IF,1)
WFUN=BFJ-1/SQRT(P*X)+X

-COP /POL/ TO TPT

AR=1

ЗØ

```
С
      REFLECTOR POLARIZATION LOSS
C
       J1(PU)/PU FEED PATTERN
С
       USES DOUBLE SIMPSON AND ROMBERG INTEGRATIONS
       INSERT D(IAMETER) VECTOR FOR DESIRED EDGE TAPER
C
      DIMENSION D(8)
       COMMON W
       DISPLAY /
       DATA D/2.516,1.697,1.293,1.054,.894,.777,.681,.586/
200
      P=3.1415926536
       A=B=Ø
       N=6
       M = 2
       MS=8
      L=3
       I = \emptyset
       TS=20
       TD = 10
       TSR=TS*P/180
       TDR=TD*P/180
       U = \emptyset
       V=TSA
       DO 100 TH=TS.90 TD
       I=I+1
       W=P*D(I)
       THA=TH*P/180
       M = MM
       IF (TH.EQ.TS) MM=MS
       CALL SIMPDB(Ø...5*P.N.U.V.MM.AA)
       A = A + AA
       CALL ROMB (U.V.L.BB)
       U=U+TDR
       IF (TH.EQ.TS) U=TSR
       V=V+TDR
       B=B+.5*P*8B
       ETA=(A/B)**2
       DB=10*ALOG10(ETA)
       FOD=.25*COS(.5*THR)/SIN(.5*THR)
100
       WRITE (1,105) TH,FOD,ETA,DB
       DISPLAY /
105
       FORMAT (F6.0.3F7.3)
       END
       FUNCTION FCT(X,Y)
       COMMON W
       AR=W*SIN(Y)
       IF (AR.LT..001) GO TO 30
                                                   50
       CALL BESSEL(AR.1.BF.IF.1)
       F=2*BF/AR
       GO TO 40
```

-COP /CASS/ TO TPT

```
С
       CASSEGRAIN PARAMETERS
       DISPLAY /
       ACCEPT "MAG ",XM
DO 110 FD=.25,.5,.05
100
       DISPLAY
       FE=XM*FD
       A=16*XM*FD*FD
       DSDØ=A/((XM+1)*(A-1))
DISPLAY "FOD,FED,DSDØ
                                    ",FD,FE,DSDØ,/
       DO 110 DSD=.05..3..05
       F2=D5D*(A-1)/A
       F1=XM*F2
       FP=F1+F2
       WRITE (1,150) DSD,F1,F2,FP
110
150
       FORMAT (4F8.3)
       DISPLAY /./
       GO TO 100
       END
```

```
In fitt=F
                                               Dslb
                         fe/p
MAG
                f/D
                                                W
                         Ø.25
                Ø.25
FOD FED
            filt
   Ds/D
             N.NNN
                               0.000
                      0.000
   0.050
                               0.000
                      0.000
             Ø.UØØ
   0.100
                               0.000
                      0.000
   0.150
             0.000
                      0.000
                               0.000
             0.000
   0.200
                      0.000
                               0.000
             0.000
   0.250
                               0.000
                      0.000
             0.000
   0.300
                                               1,636
                        Ø.3
FOD, FED
                Ø.3
                      0.015
                               Ø. Ø31
             Ø.Ø15
   0.050
                               0.061
                      0.031
   0.100
             0.031
                               0.092
                      0.046
   0.150
             0.046
                      0.061
                               Ø.122
             0.061
    0.200
                      0.076
                               0.153
             0.076
    0.250
                      0.092
                                Ø.183
    0.300
             0.092
                                              1,021
                          Ø.35
                Ø.35
FOD, FED
                                0,049
                      0.024
    0.050
             0.024
                                0.098
                      0.049
             0.049
    0.100
                               0.147
                      0.073
             0.073
    0.150
                                0.196
                      0.098
    0.200
             0.098
                                0.245
                      0.122
             0.122
    0.250
                                Ø.294
                      0.147
             0.147
    0.300
                                              8205
                         0.4
                 0.4
FOD.FED
                                0.061
                      0.030
             0.030
    0.050
                                0.122
                       0.061
             0.061
    0.100
                                Ø.183
                       0.091
    0.150
             0.091
                       Ø.122
                                0.244
             Ø.122
    Ø.200
                                Ø.3Ø5
                       Ø.152
    Ø.250
             Ø.152
                                Ø.366
              Ø.183
                       0.183
    0.300
                                               .૧૪૪૨
                          0.45
                 0.45
FOD. FED
                                Ø.069
             0.035
                       0.035
    0.050
                       0.069
                                Ø.138
              0.069
    0.100
                                0.207
                       0.104
    0.150
              0.104
              Ø.138
                       Ø.138
                                Ø.277
    0.200
                       Ø.173
                                Ø.346
              Ø.173
    Ø.25Ø
                                0.415
              0.207
                       0.207
    0.300
                                               6667
                 Ø.5
                         Ø.5
 FOD.FED
                                Ø.075
                       Ø. Ø37
              0.037
    0.050
                       0.075
                                0,150
              0.075
    0,100
                                Ø.225
                       Ø.113
              Ø.113
    Ø.15Ø
              0.150
                       0.150
                                0.300
     0.200
                                                           52
                                Ø.375
              Ø.187
                       Ø.187
     Ø.25Ø
                                0.450
                       Ø.225
              Ø.225
     0.300
```

Q

MAG

```
*WRI/CASS/
                                   Old File?
                                   16 Lines
                                              DS/D for (fitfz)=f
MAG
       1.5
              +/0
                        fe/D
                                   *Xtran
                                   +Test
                         Ø.375
                Ø.25
FOD FED
                                                 1.200
                              (fi+fr)/f
            FILE
                     f2/F
   Ds/D
                               0.042
            0.025
   0.050
                      Ø. Ø 17
                               0.083
            0.050
                      0.033
   0.100
                               Ø.125
            0.075
                      0.050
   0.150
                               0.167
   0.200
             0.100
                      0.067
                               0.208
   Ø.25Ø
             Ø.125
                      0.083
             0.150
                      0.100
                               Ø.25Ø
   0.300
                                               ,7448
                Ø.3
                        0.45
FOD FED
             0.040
                      0.027
                               0.067
   0.050
                               Ø.134
   0.100
             Ø.Ø81
                      0.054
                               0.201
                      0.081
   0.150
             0.121
                      0.107
                               0.269
   0.200
             Ø.161
             0.201
                      Ø.134
                               Ø.336
    Ø.25Ø
                               0.403
             0.242
                      Ø.161
    0.300
                                              6062
                Ø.35
                         Ø.525
FOD FED
             0.049
                               0.082
                      0.033
    0.050
                               0.165
             0.099
                      0,066
   0.100
                      0.099
                               0.247
    0.150
             0.148
    0.200
             Ø.198
                      0.132
                               Ø.33Ø
                      Ø.165
                               0.412
    0.250
             0.247
                      Ø.198
                               0.495
    0.300
             0.297
                                            5408
                        0.6
                0.4
FOD.FED
                      0,037
                               0.092
    0.050
             0.055
                      0.074
                               Ø.185
             Ø.111
    0.100
                               0.277
    Ø.15Ø
             Ø.166
                      0.111
                      Ø.148
                               Ø.37Ø
             Ø.222
    0.200
                      Ø.185
                               0.462
    0.250
             Ø.277
                               0.555
                      Ø.222
    0.300
             Ø.333
                                             5036
                          Ø.675
                0.45
FOD, FED
             0.060
                      0.040
                               0.099
    0.050
                      0.079
                               Ø.199
             Ø.119
    0.100
                               Ø.29B
             Ø.179
                      0.119
    0.150
                               Ø.397
                      0.159
             Ø.238
    0.200
                      Ø.199
             Ø.298
                               0.496
    0.250
                                0.596
                      Ø.238
    0.300
             Ø.357
                         Ø.75
                                               4800
                0.5
FOD, FED
                      0.042
                                0.104
             0.062
    0.050
                                0.208
    0.100
             Ø.125
                      0,083
             Ø.187
                      0,125
                                0.312
    0.150
             0.250
                                Ø.417
                      Ø, 167
    0.200
                                0.521
    0.250
             0.312
                       0.208
                                                                 Sil
                       0.250
                                Ø.625
             Ø.375
    0.300
```

MAG

```
MAG
      2
                                        0.666666667
                      Ø.25
                               0.5
FOD_FED_DSDØ
   0.050
            0.050
                      0.025
                               0.075
            Ø.100
                      0.050
                               0.150
   0.100
   0.150
            0.150
                      0.075
                               0.225
   0.200
            0.200
                      0.100
                               0.300
   Ø.250
            Ø.25Ø
                      0.125
                               0.375
   0.300
            0.300
                      0.150
                               0.450
                      Ø.3
                              Ø.6.
                                      0.510638298
FOD FED DSDØ
   0.050
            0.065
                      0.033
                               0.098
                               0.196
   0.100
            Ø,131
                      0.065
                               0.294
   Ø.15Ø
            0.196
                      0.098
   Ø.200
            Ø.261
                      0.131
                               0.392
   Ø.25Ø
                      0.163
                               0.490
            Ø.326
                      0.196
                               Ø.587
   0.300
            Ø.392
FOD, FED, DSDØ
                      Ø.35
                               0.7
                                        0.447488584
                      0.037
                               0.112
   0.050
            0.074
   0.100
            0,149
                      0.074
                               Ø.223
   0.150
            Ø.223
                      0.112
                               0.335
                      Ø.149
                               0.447
   0.200
            Ø.298
   0.250
             0.372
                      0,186
                               Ø.559
                      0.223
                               0.670
   0.300
            0.447
                      0.4
                              0.8
                                      0.414239482
FOD.FED.DSDØ
                               0.121
   0.050
            0.080
                      0.040
                               Ø.241
   0.100
             0.161
                      0.080
   Ø.15Ø
            0.241
                      Ø.121
                               Ø.362
                               Ø.483
   0.200
            0.322
                      Ø.161
                               0.604
   0.250
             0.402
                      0.201
                      Ø.241
   0.300
            Ø.483
                               Ø.724
                                        0.394160584
FOD.FED.DSDØ
                      0.45
                               0.9
                      0.042
                               Ø.127
   0.050
             0.085
   0.100
             0.169
                      0.085
                               0.254
                               Ø.381
             0.254
                      Ø.127
   0.150
                      0,169
                               0,507
   0.200
             0.338
                      Ø.211
   0.250
             Ø.423
                               0.634
   0.300
             0.507
                      Ø.254
                               0.761
                                    0.380952381
FOD FED DSD0
                      \emptyset . 5
   0.050
                      0.044
                               Ø,131
             0.087
   0.100
             Ø.175
                      0.087
                               0.262
                      0,131
                               0.394
   0.150
             Ø.262
                               Ø.525
   0.200
             0.350
                      Ø.175
```

0.219

0.262

0.250

0.300

Ø.437

Ø.525

Ø.656

0.787

•				
FOD, FED, DS	DØ	0.25	Ø.75	0.375
0.050 0.100 0.150 0.200 0.250 0.300	0.200 0.300 0.400 0.500	0.033 0.067 0.100 0.133 0.167 0.200	0.133 0.267 0.400 0.533 0.667 0.800	
FOD, FED, DS	SD Ø	Ø.3	Ø.9	Ø.3253Ø12Ø5
0.100 0.150 0.200 0.250		0.192	Ø.615 Ø.769	
FOD, FED, DE	SOØ	0.35	1.05	0.301229508
0.100 0.150 0.200 0.250	0.124 0.249 0.373 0.498 0.622 0.747	Ø.083 Ø.124 Ø.166 Ø.207	0.830	
FOD, FED, DS	BDØ .	0.4	1.2	Ø.28742515
Ø.150 Ø.200	Ø.13Ø Ø.261 Ø.391 Ø.522 Ø.652 Ø.783	Ø.Ø87 Ø.13Ø Ø.174	0.174 0.348 0.522 0.696 0.870 1.044	1 .
FOD, FED. DS	SD Ø	0.45	1.35	ø.278669725
0.100 0.150 0.200 0.250	0.135 0.269 0.404 0.538 0.673 0.807	Ø.045 Ø.090 Ø.135 Ø.179 Ø.224 Ø.269	Ø.359 Ø.538 Ø.718 Ø.897	
FOD, FED, DS	SDØ	Ø.5	1.5	0.272727273
0.200 0.250	0.137 0.275 0.412 0.550 0.687 0.825	Ø.183 Ø.229	0.367	

MAG 5				. 03
FOD, FED	0.25	1.25		,2083
0.050 0.100 0.150 0.200 0.250 0.300	0.200 0.400 0.600 0.800 1.000 1.200	0.040 0.080 0.120 0.160 0.200 0.240	0.240 0.480 0.720 0.960 1.200 1.440	
FOD, FED	Ø.3	1.5	-	.1935
0.050 0.100 0.150 0.200 0.250	0.215 0.431 0.646 0.861 1.076 1.292	Ø.043 Ø.086 Ø.129 Ø.172 Ø.215 Ø.258	Ø.258 Ø.517 Ø.775 1.033 1.292 1.550	
FOD.FED	Ø.35	1.75		1856
Ø.050 Ø.100 Ø.150 Ø.200 Ø.250 Ø.300	Ø.224 Ø.449 Ø.673 Ø.898 1.122	Ø.Ø45 Ø.Ø9Ø Ø.135 Ø.18Ø Ø.224 Ø.269	Ø.269 Ø.539 Ø.8Ø8 1.078 1.347	
FOD, FED	Ø . 4	2		1808
0.050 0.100 0.150 0.200 0.250 0.300	0.230 0.461 0.691 0.922 1.152 1.383	Ø.046 Ø.092 Ø.138 Ø.184 Ø.23Ø Ø.277	Ø.277 Ø.553 Ø.83Ø 1.106 1.383 1.659	
FOD, FED	0.45	2.25		. 1776
0.050 0.100 0.150 0.200 0.250 0.300	0.235 0.469 0.704 0.938 1.173	Ø.Ø47 Ø.Ø94 Ø.141 Ø.188 Ø.235 Ø.281	0.281 0.563 0.844 1.126 1.407	
FOD,FED	0.5	2.5		.1754
0.050 0.100 0.150 0.200 0.250 0.300	0.238 0.475 0.712 0.950 1.187	0.047 0.095 0.143 0.190 0.237 0.285	0.285 0.570 0.855 1.140 1.425 1.710	

			•		. •
MAG	7	•		•	
FOD.	FED.DS	D Ø	Ø.25	1.75	0.145833333
	ara	a saa	6 842 ·	מ אים	
	050	Ø.300	0.043		
	100	0.600	0,086	0.686	
	.150	0.900	Ø.129	1.029	•
	.200	1.200	0.171	1.371	•
	.250		Ø.214		
2	.300	1.800	Ø.257	2.057	
FOD.	FED, DS	50 Ø	0.3	2.1	Ø.13876652
0	•050	0.315	0.045	0.360	
	100	Ø.631	0.090	0.721	
		- 0.946	Ø.135	1.081	
		1.261	0.180		-
		1.576	0,225	1.802.	
	300	1.892	Ø.27Ø	1.441 1.802 2.162	
	FED.DS	Sdø	Ø.35	2.45	0.134827044
				;	•
	.050	0.324	0.046		
Ø	1.100	0.649	0.093	0.742 1.113 1.483	
. 6	.150	0.973	Ø.139	1,113	
· · · · · · · · · · · · · · · · · · ·	,200	1.298	Ø.185	1.483	
	.250	1.622	Ø.232	1.854	
E	300	1.947	Ø.278	2.225	
FOD,	FED.DS	SDØ .	0.4	2.8	Ø.1323877Ø7
_		a 00a	a a.a.	4 250	
	1.050	0.330		Ø.378	
	1.100	0.661	0.094	Ø.755	
	1.150		Ø.142		
	1.200		Ø.189		
	1.250	1.652	Ø.236	1,888	•
(3.300	1.983	0.283	2.266	
FOD,	,FED,D	SD Ø	0.45	3.15	Ø.130765683
	0.Ø5Ø	0.335	0.048	Ø.382	,
	1.10U	a 669°	0.096	Ø.765	
	0.15Ø	1.004		1,147	
	200	1.338	Ø.191	1.529	
		1.673			
	0.250 0.300		Ø.287		
	FED.D	•	Ø.5	3.5	Ø.12962963
		•		•	
	0.050	Ø.337	0.048	0.386	
	0.100		0.096		
1	8.150	1.013	0.145	1.157	
1	0.200	1.350	0.193	1.543	•
1	0.250	1,687	0.241	1.929	
	0.300	2.025	Ø.289	2.314	
					•

FOD.FED.DSDØ	0.25	2.5	0.101010101
Ø.050 Ø.450 Ø.100 Ø.900 Ø.150 1.350 Ø.200 1.800 Ø.250 2.250 Ø.300 2.700	0.090 0.135 0.180 0.225	0.990 1.485 1.980 2.475	
FOD, FED, DSDØ	0.3	3 Ø.	.097693351
0.050 0.465 0.100 0.931 0.150 1.396 0.200 1.861 0.250 2.326 0.300 2.792	Ø.093 Ø.140 Ø.186 Ø.233		
FOD.FED.DSDØ	Ø.35	3.5	Ø.095796676
0.150 1.423 0.200 1.898 0.250 2.372	Ø.095 Ø.142 Ø.190	1.566 2.088 2.610	· ·
	· .		
FOD.FED.DSDØ	0.4	4 0.	,094604582
### ##################################	0.048 0.096 0.144 0.192 0.240	Ø.529	,094604582
0.050 0.480 0.100 0.961 0.150 1.441 0.200 1.922 0.250 2.402	0.048 0.096 0.144 0.192 0.240	0.529 1.057 1.586 2.114 2.643	0.093804285
Ø.050 Ø.480 Ø.100 Ø.961 Ø.150 1.441 Ø.200 1.922 Ø.250 2.402 Ø.300 2.883	0.048 0.096 0.144 0.192 0.240 0.288 0.45 0.45 0.097 0.194 0.194 0.242	0.529 1.057 1.586 2.114 2.643 3.171	
0.050 0.480 0.100 0.961 0.150 1.441 0.200 1.922 0.250 2.402 0.300 2.883 FOD.FED.DSD0 0.050 0.485 0.100 0.969 0.150 1.454 0.200 1.938 0.250 2.423	0.048 0.096 0.144 0.192 0.240 0.288 0.45 0.45 0.097 0.194 0.194 0.242	0.529 1.057 1.586 2.114 2.643 3.171 4.5 0.533 1.066 1.599 2.132 2.665 3.198	

MAG --

ESC: (\$MAIN\$)100+